

Verifying Concurrent Turing Machines

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June 4, 2012

Internship Started
working with Arie and Sagar

June 4, 2012

Topic:

“Time-bounded Analysis of Real-time Systems”

June 4, 2012

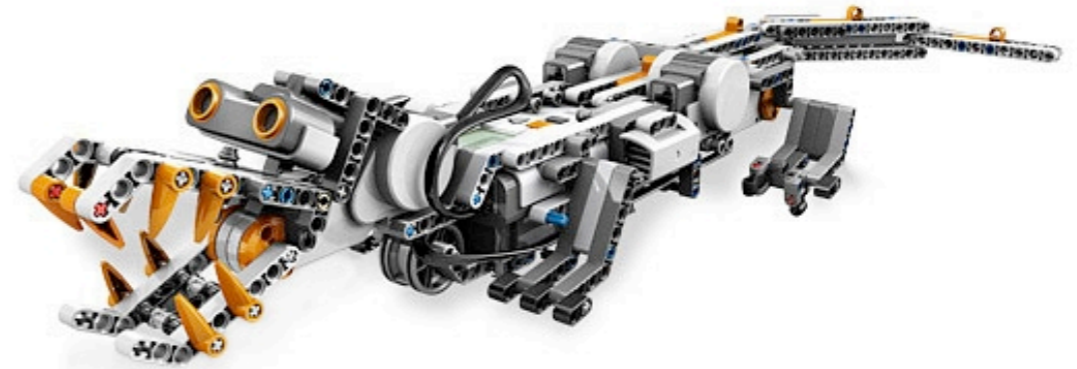
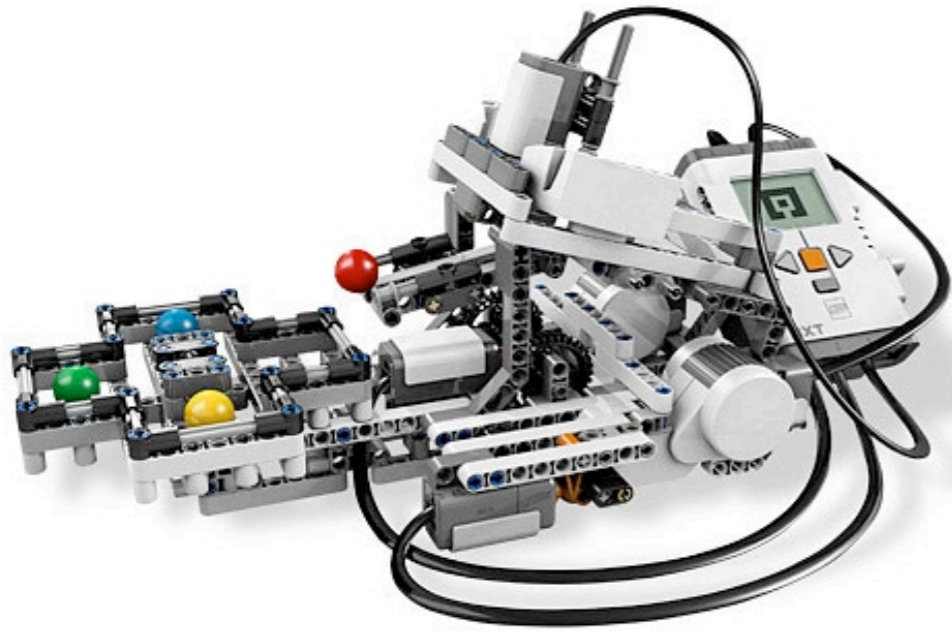
Verification of
“Concurrent, Periodic, Real-time Embedded System”

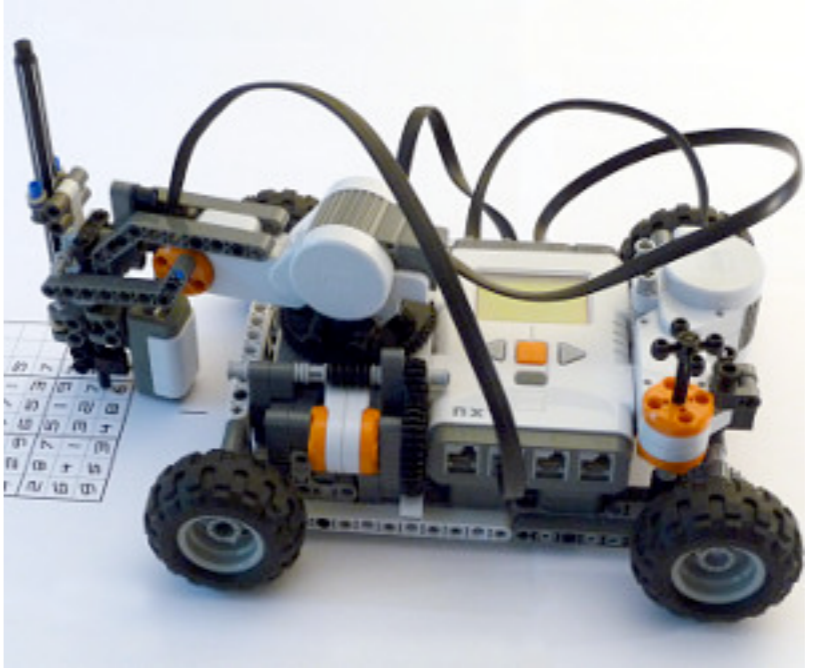
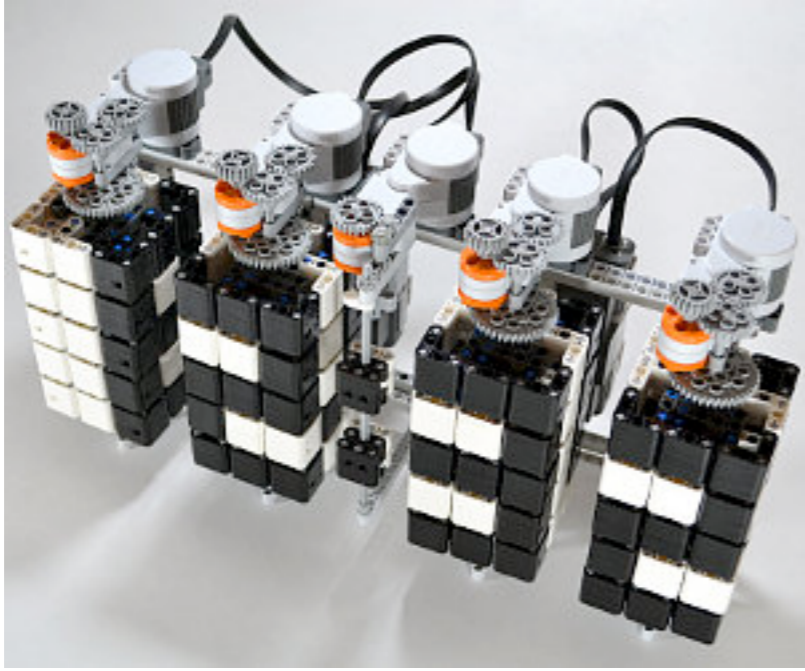
June 5, 2012



We need more examples of
concurrent systems.
Can you make one with
LEGO MINDSTORMS?







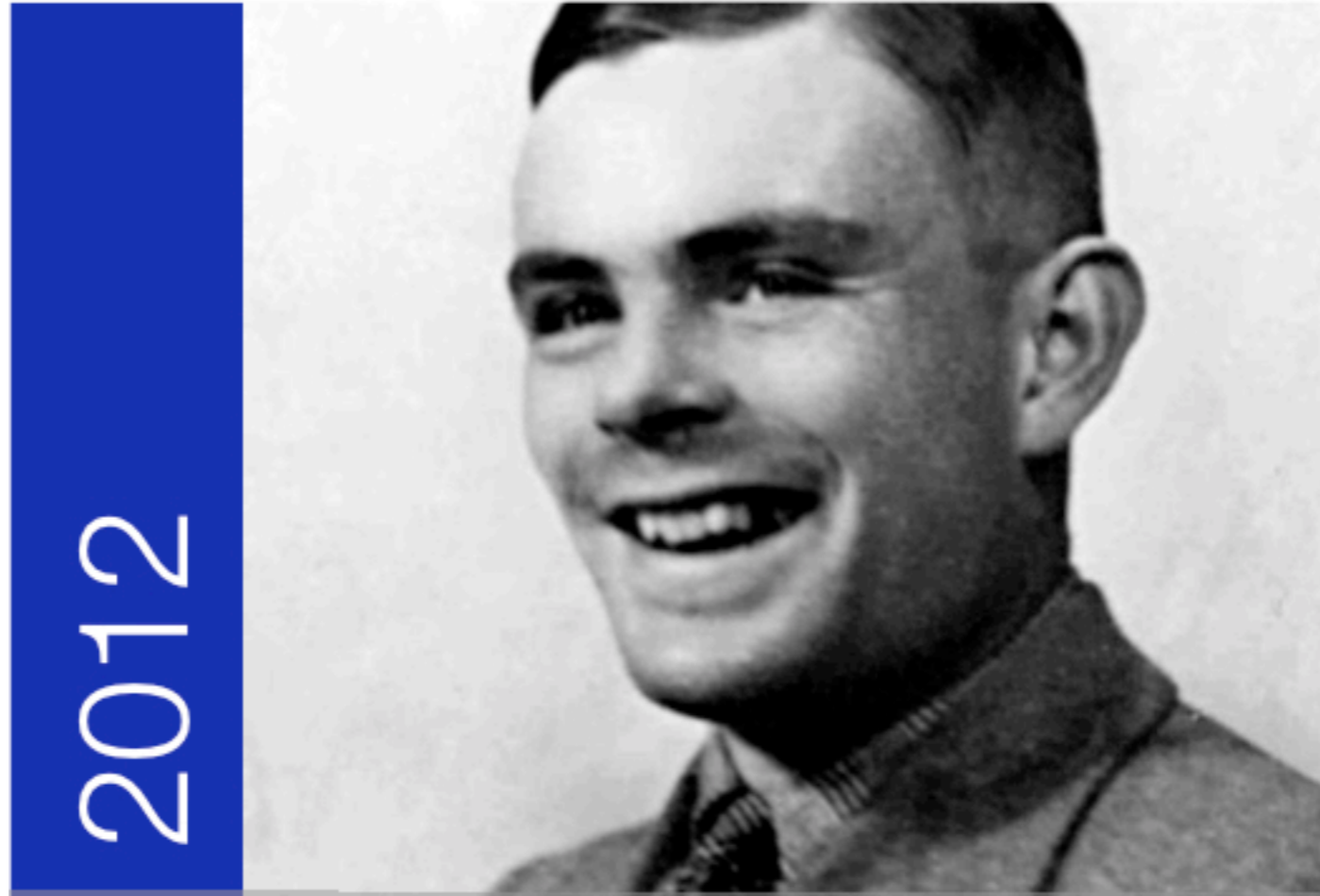
ALAN TURING YEAR

2012



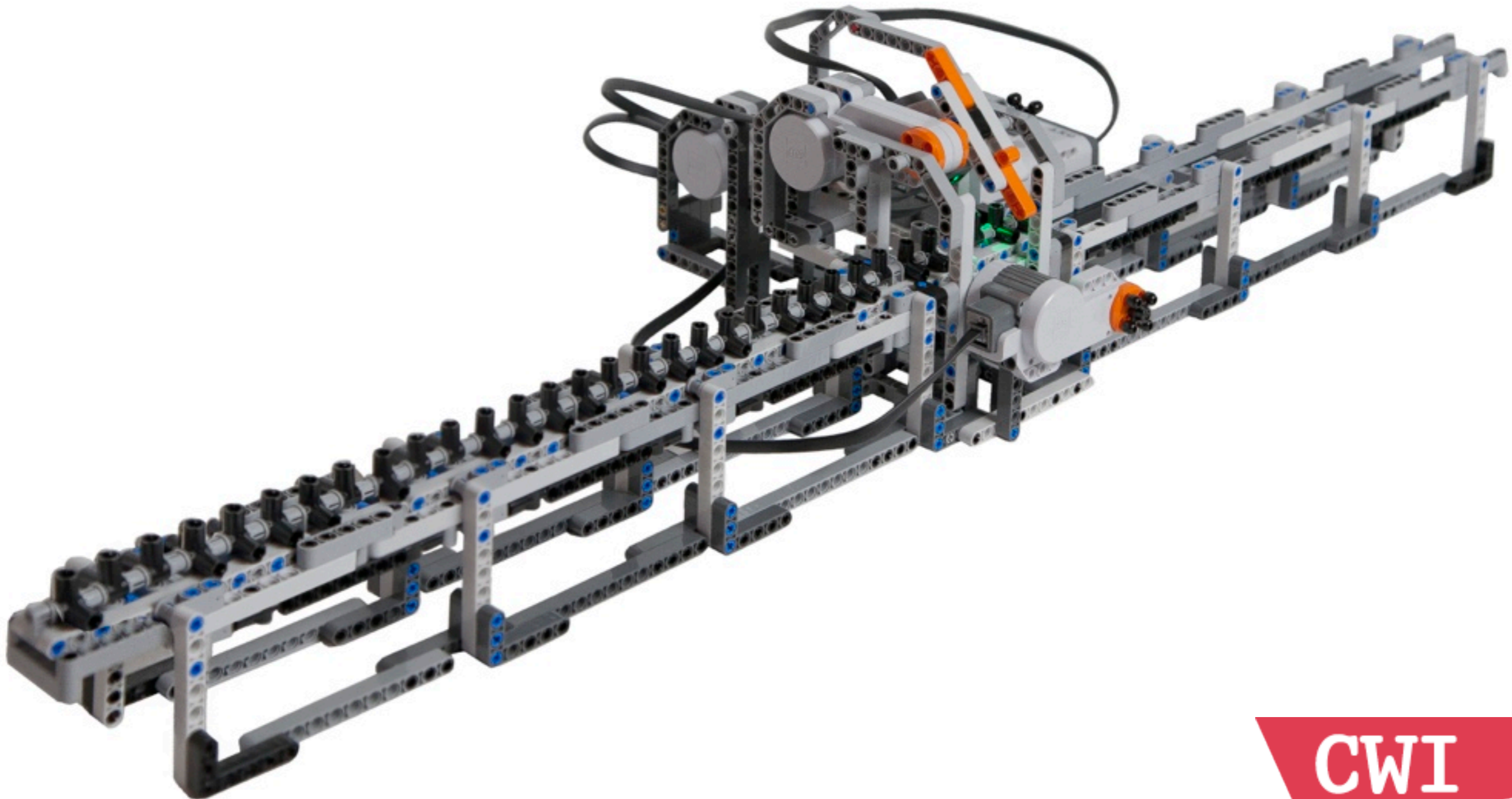
ALAN TURING YEAR

2012



LEGO Turing Machine?

A Turing Machine built using



A detailed LEGO Technic model of a tape reader/writer mechanism. The model is constructed from grey and white Technic beams and connectors, with orange and black accents. A green LED light is visible on the top left. A motor is located at the bottom right. The model is shown from a side-on perspective, highlighting the internal mechanical components.

Reader

Writer

Tape

TapeMover

CWI

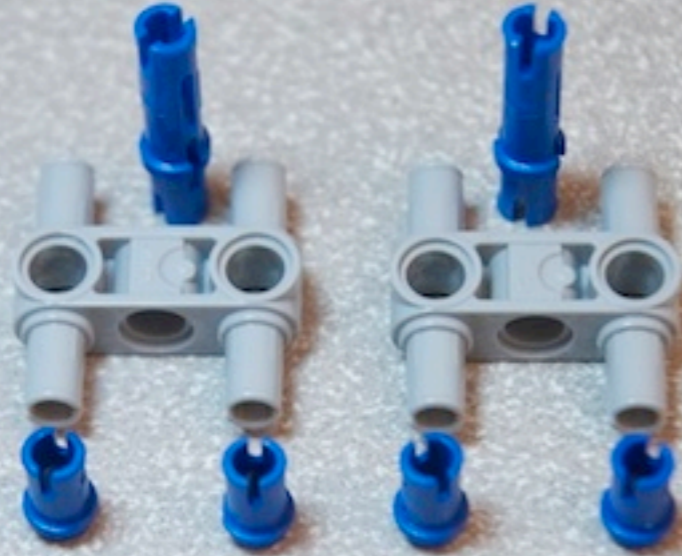
June 9, 2012



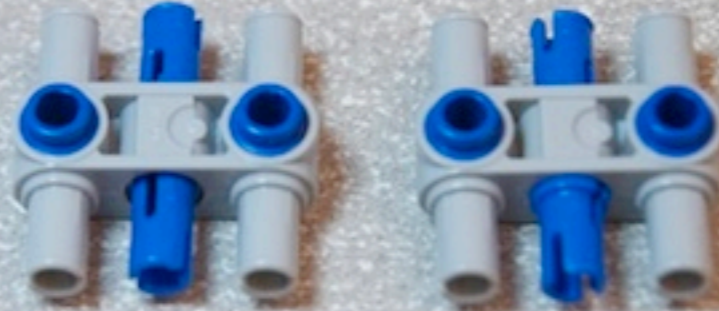
OK, Let's build one!



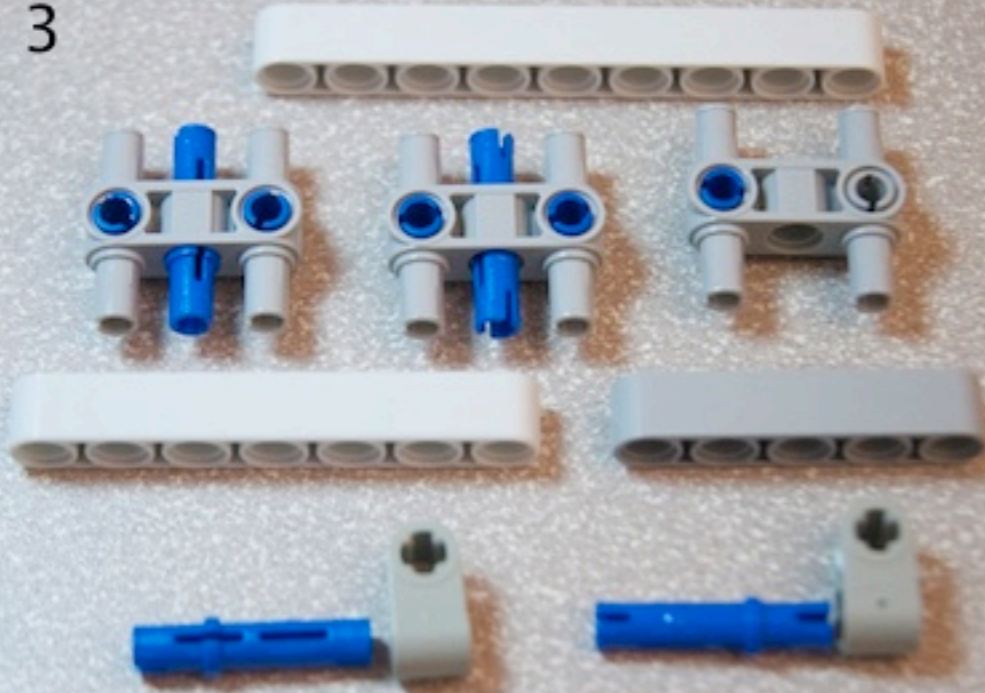
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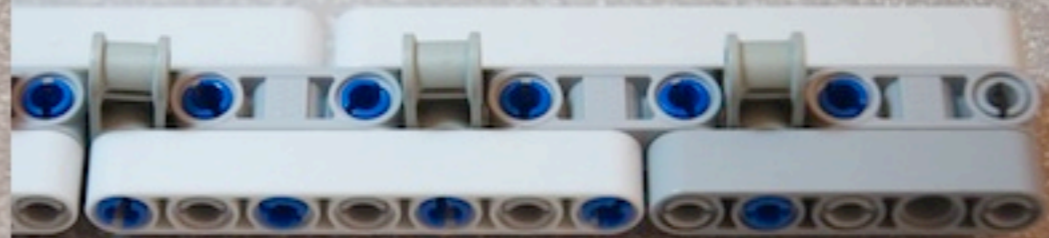
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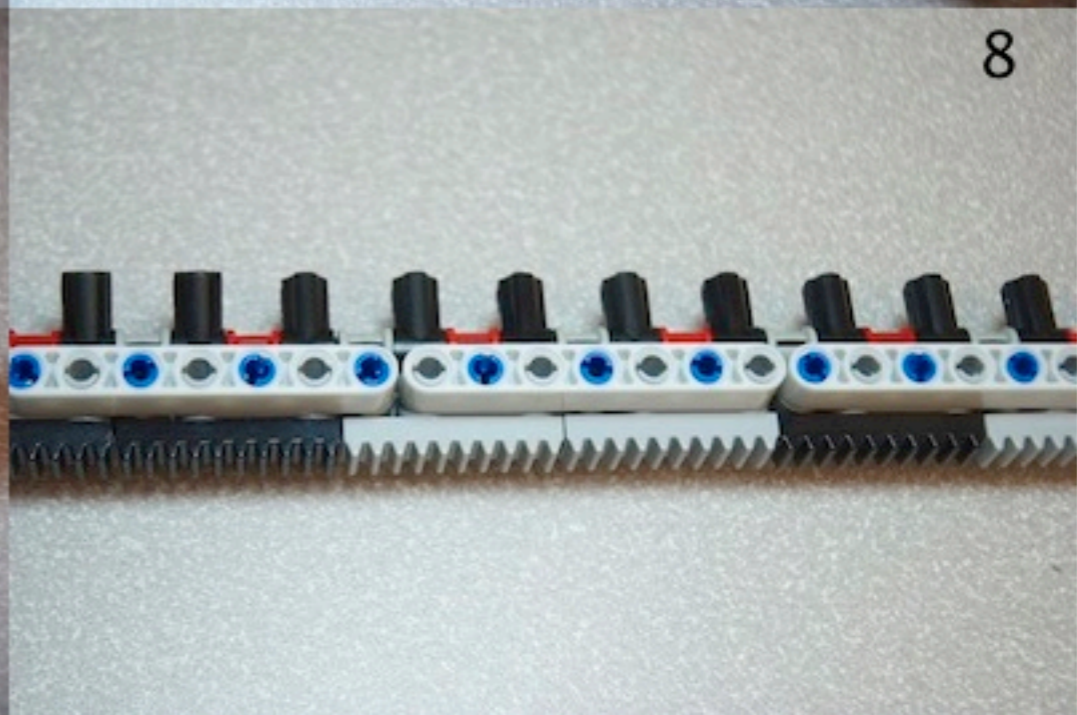
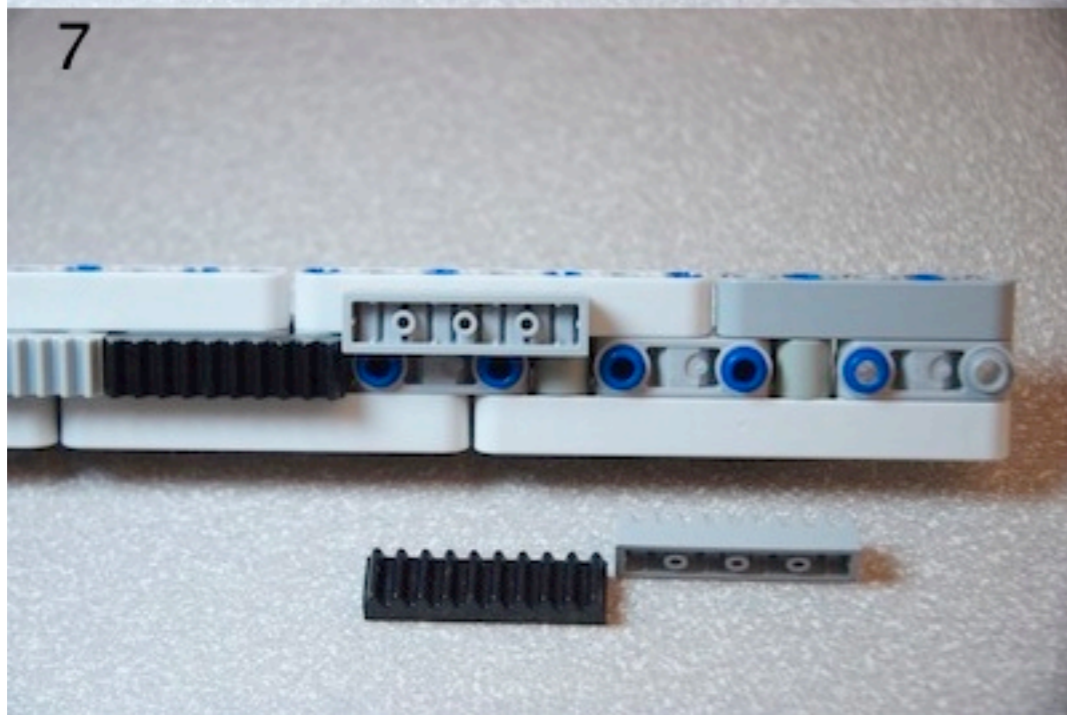
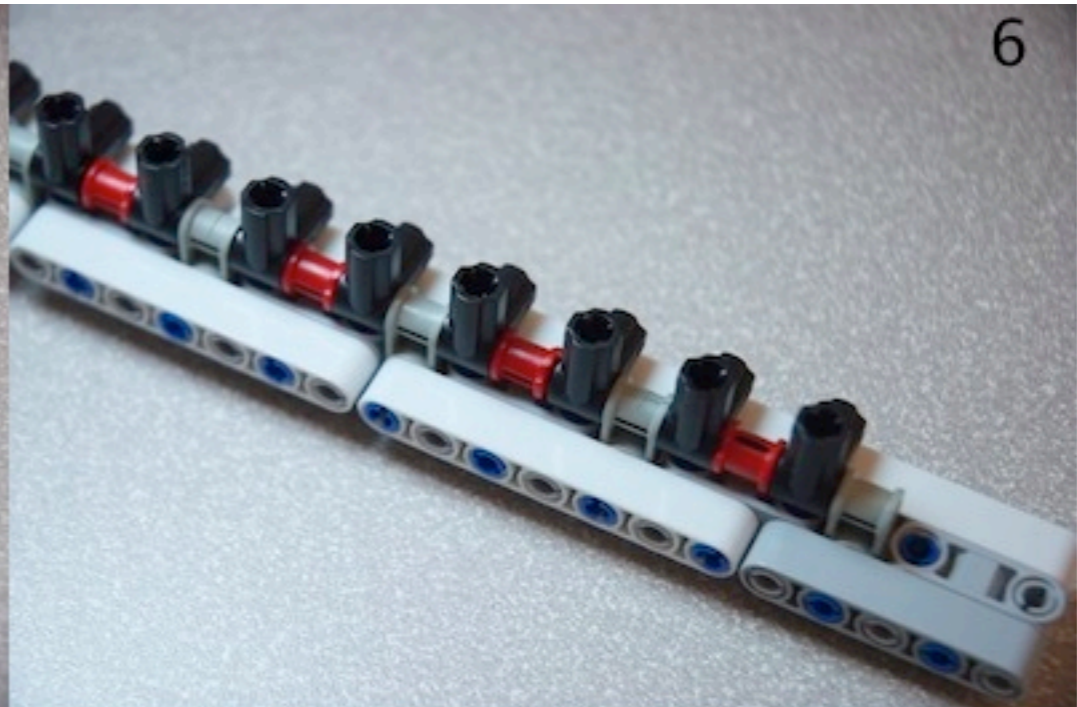
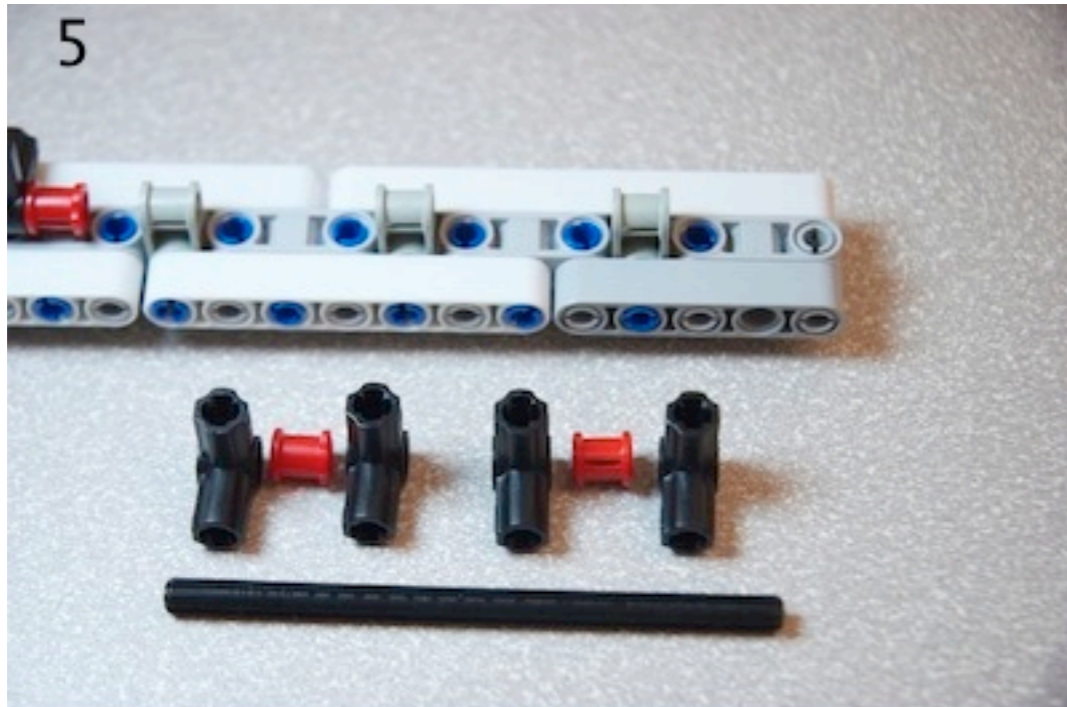


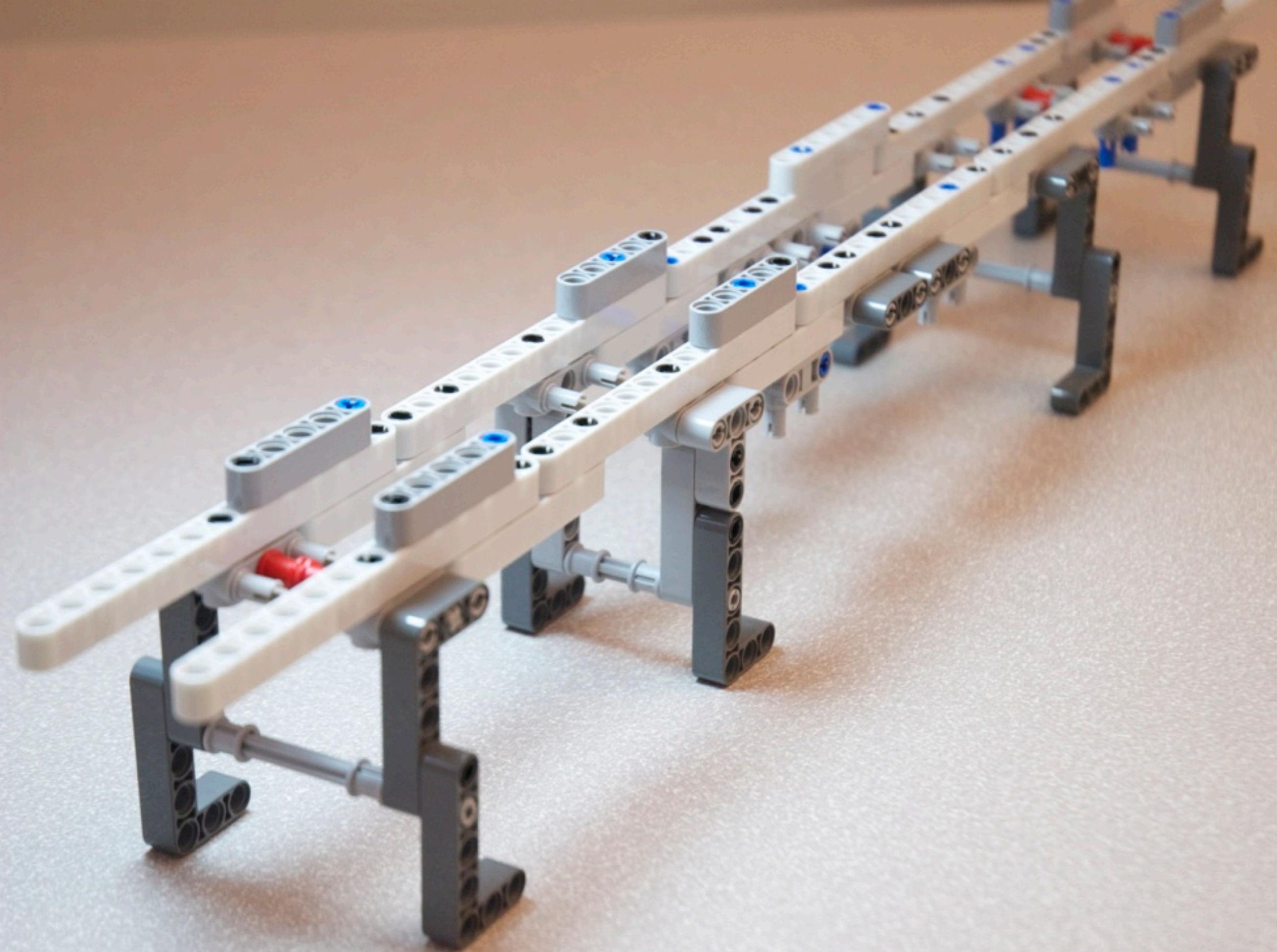
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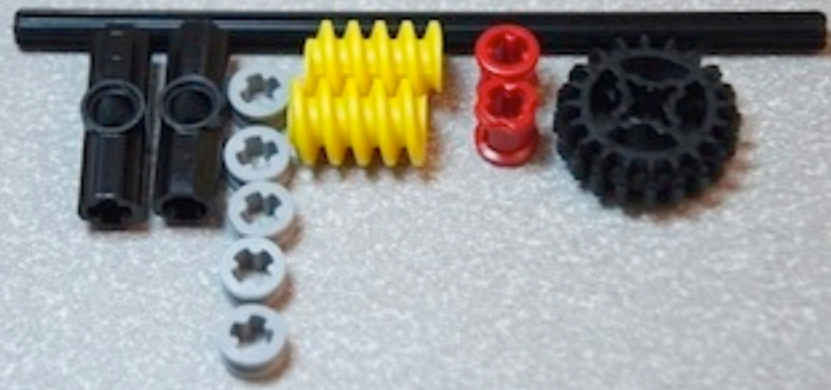
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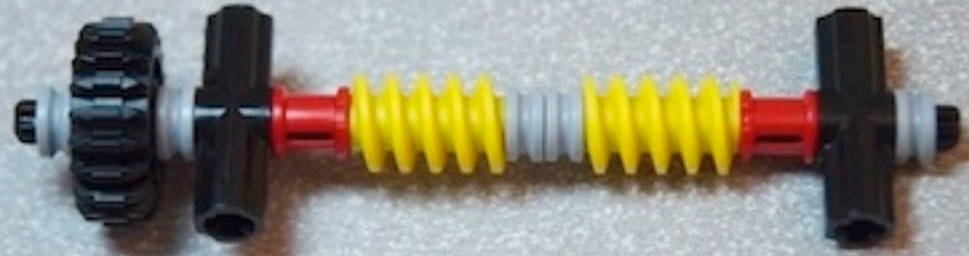




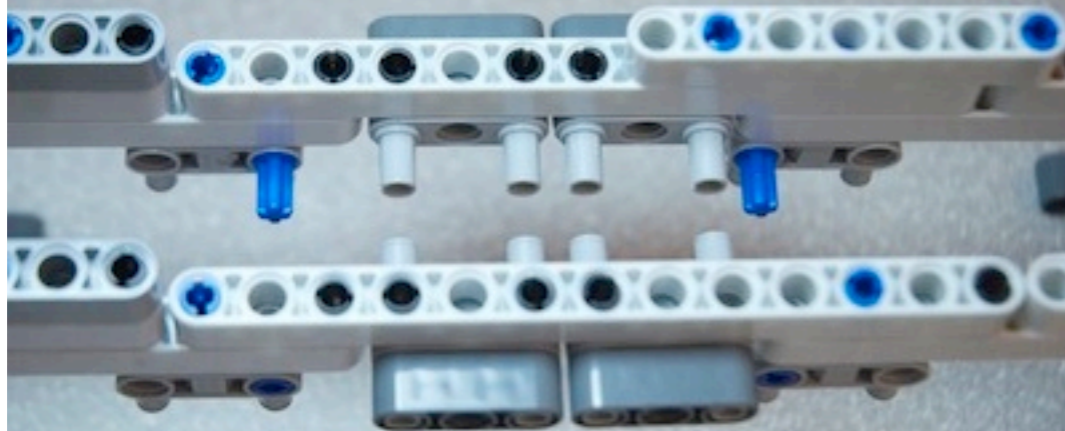
1



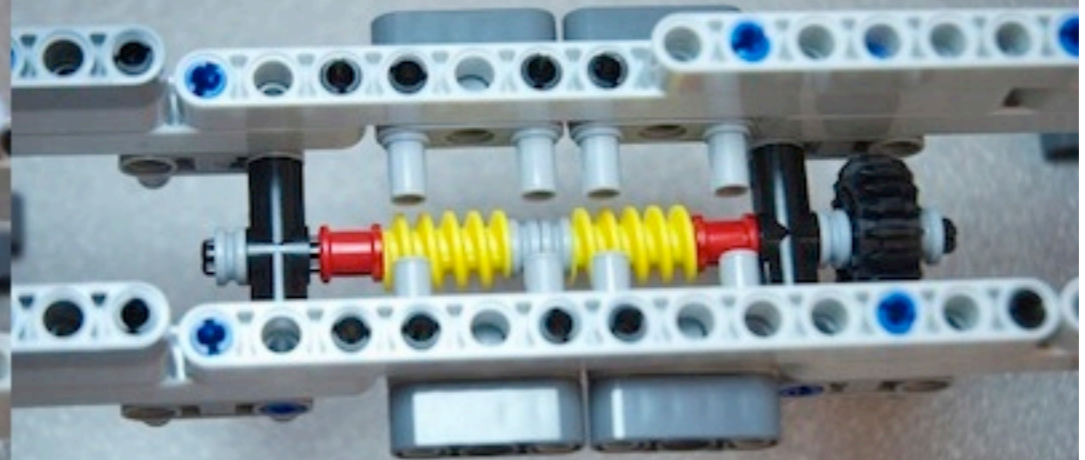
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3



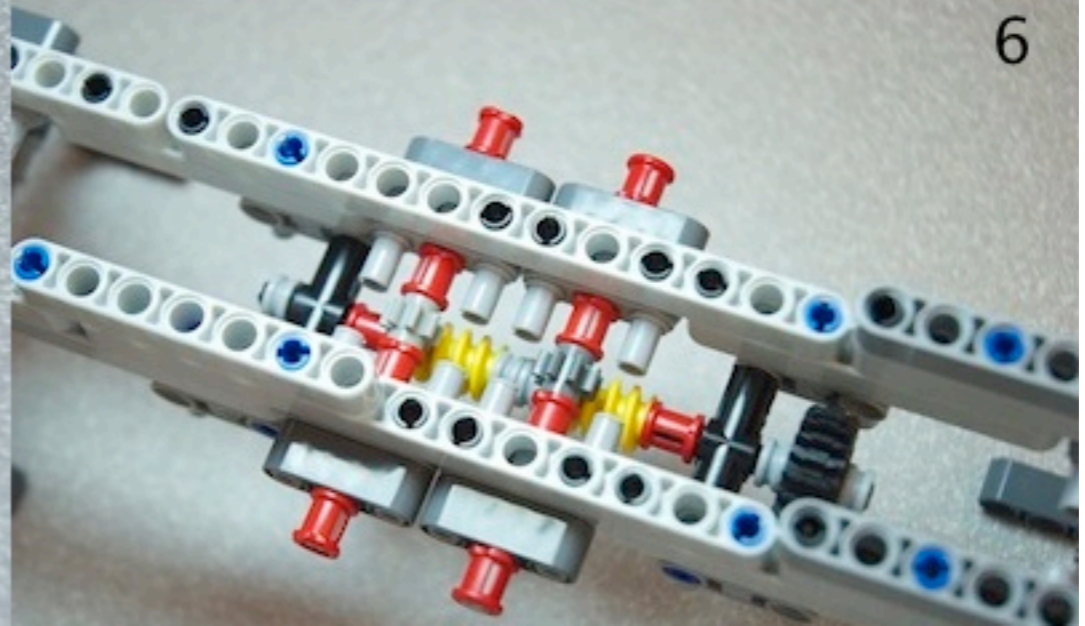
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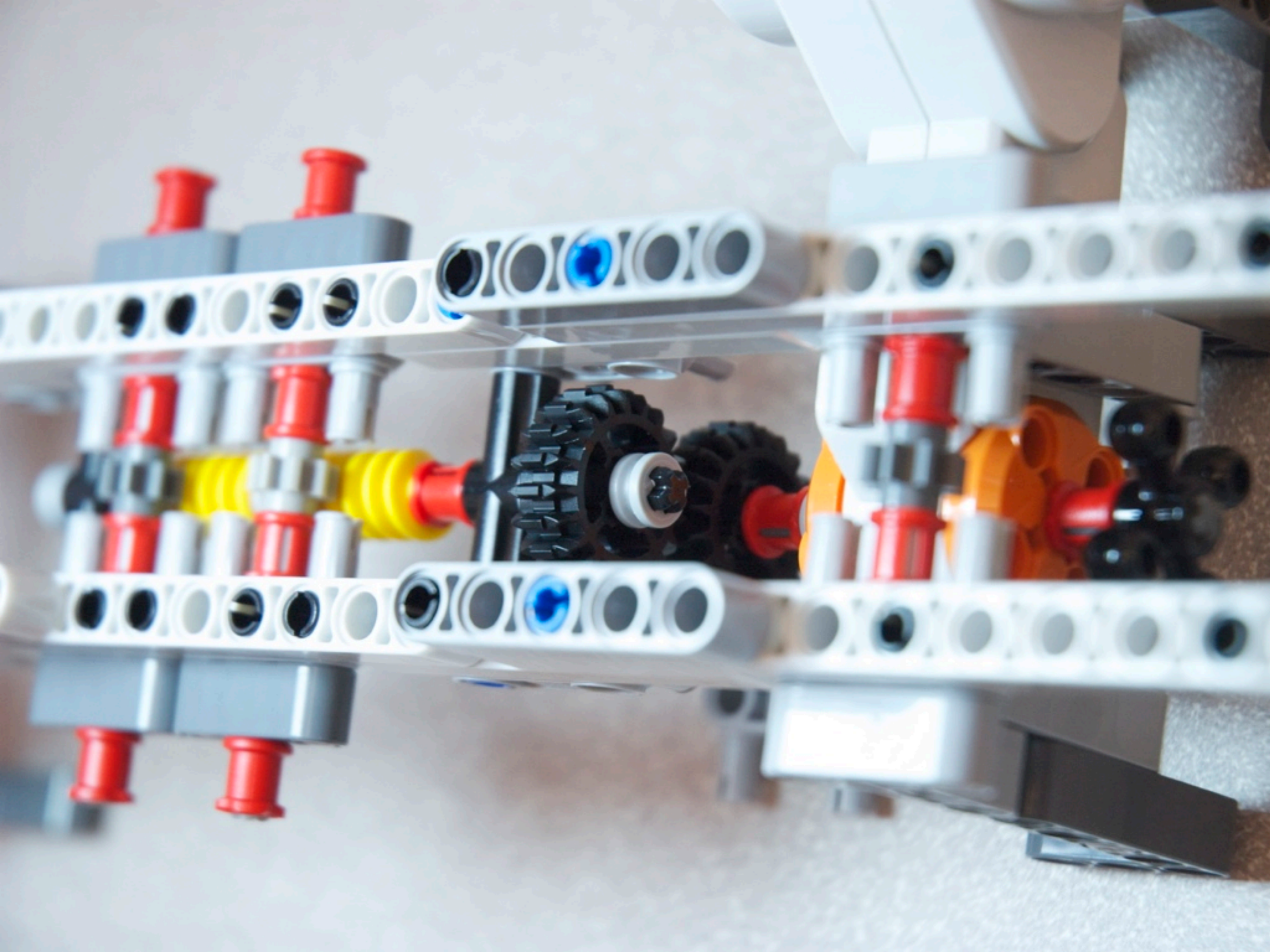


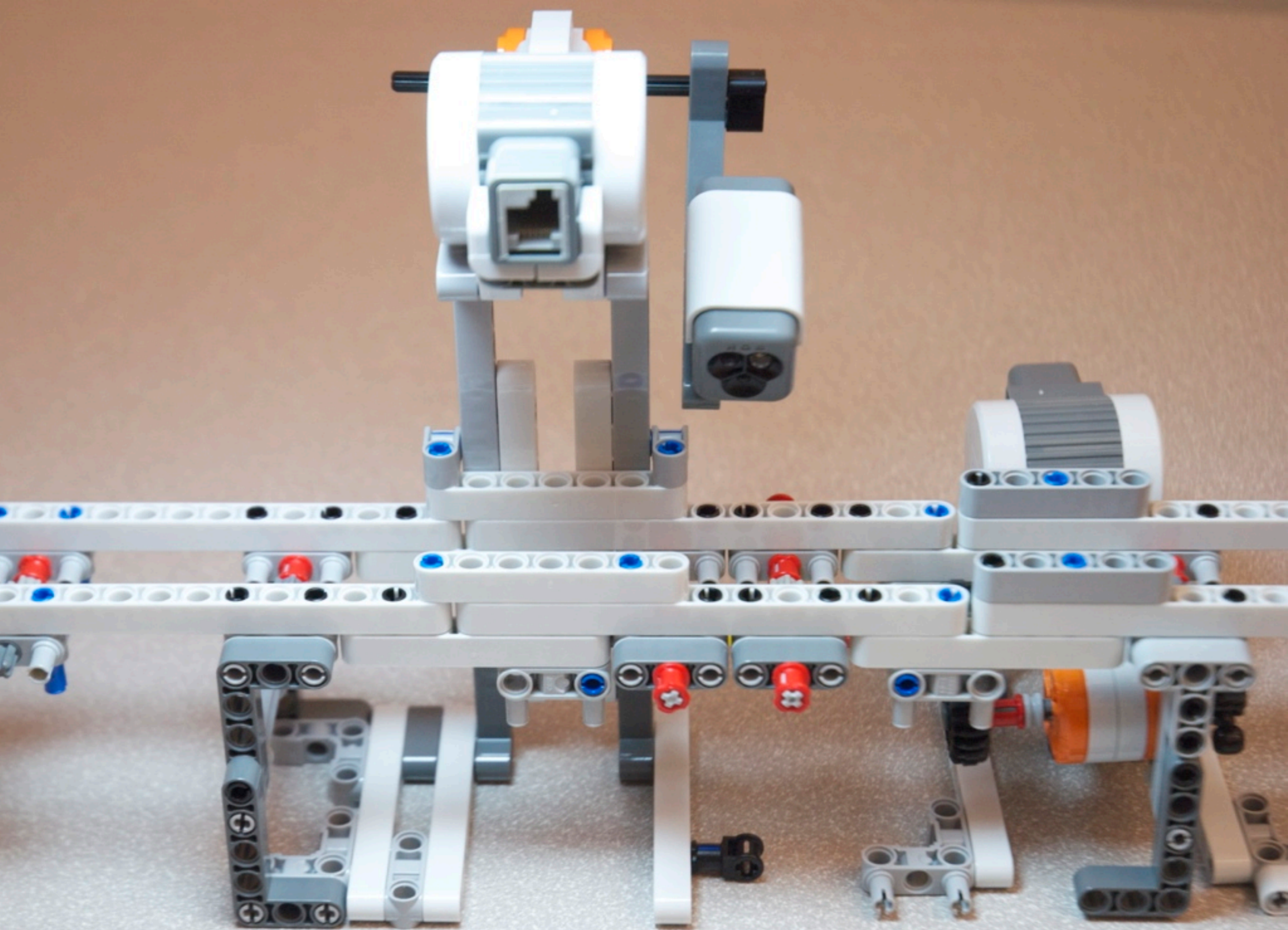
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6





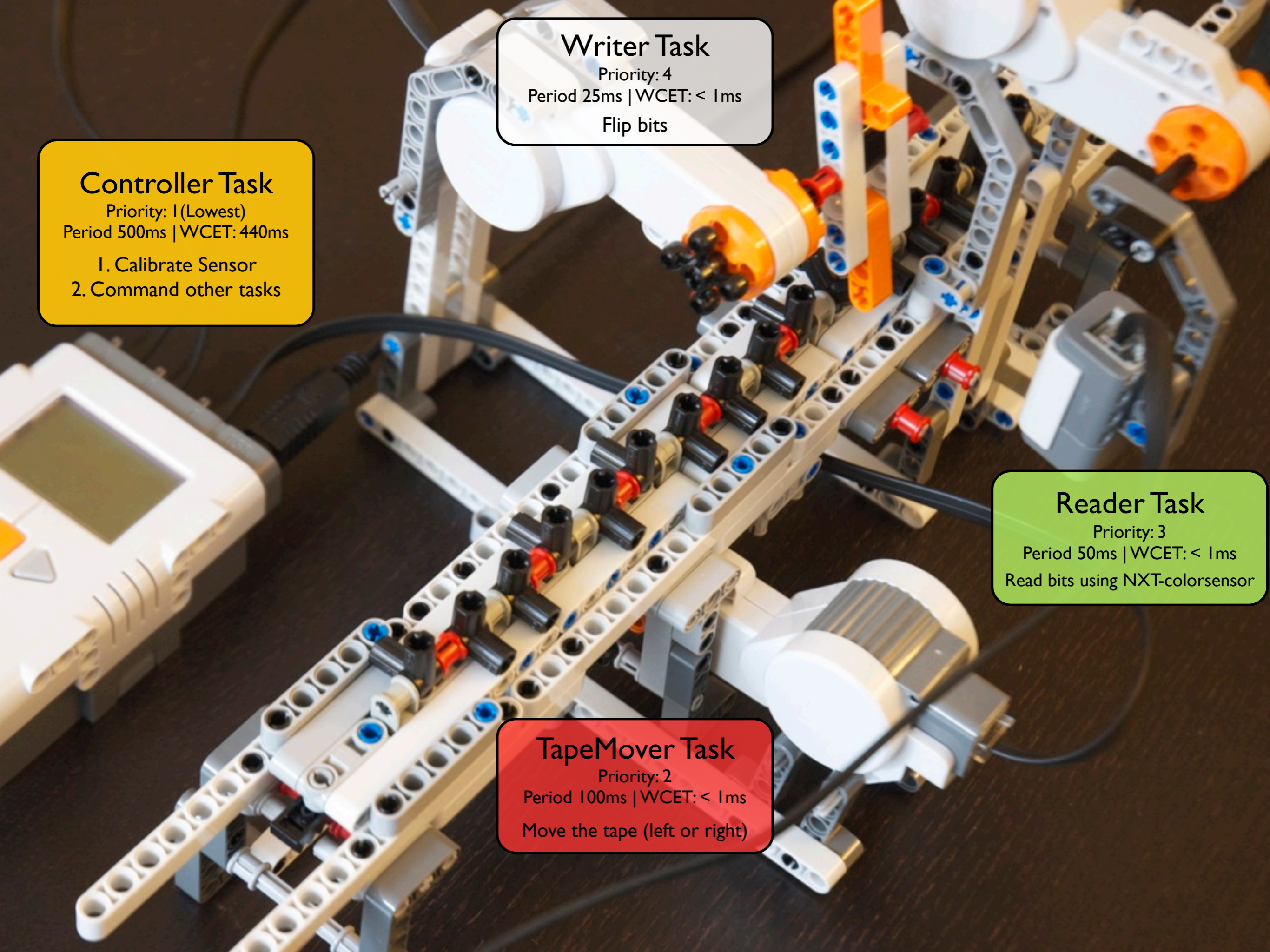






July 25, 2012
Construction Completed!

Software Implementation



Writer Task

Priority: 4

Period 25ms | WCET: < 1ms

Flip bits

Controller Task

Priority: 1 (Lowest)

Period 500ms | WCET: 440ms

1. Calibrate Sensor
2. Command other tasks

Reader Task

Priority: 3

Period 50ms | WCET: < 1ms

Read bits using NXT-colorsensor

TapeMover Task

Priority: 2

Period 100ms | WCET: < 1ms

Move the tape (left or right)

DEMO

Unary Addition

$$2 + 3 = ?$$

<http://www.youtube.com/watch?v=teDyd0d5M4o>

Properties

Property 1: When a bit is being read, all the motors should **stop**.

Property 2: When writer flips a bit, the tape motor and read motor should **stop**.

Property 3: When tape moves, the writer motor and read motor should **stop**.

Property 4: When a bit is being read, the sensor should be on **Green** mode

Property 5: The sensor mode must be switched in **Controller Task**, not in Reader Task

Properties

Property 1: When a bit is being read, all the motors should **stop**.

Property 2: When writer flips a bit, the tape motor and read motor should **stop**.

Property 3: When tape moves, the writer motor and read motor should **stop**.

Property 4: When a bit is being read, the sensor should be on **Green** mode

Property 5: The

```
case READ_SENSOR:
    if(!R(need_to_run_nxtbg)) {
#ifdef VERIFICATION
        /* Property 1: When a bit is being read,
           all the motors should be stopped. */
        /* PASSED with 4 hyper-periods */
        assert(R(R_speed) == 0 && R(W_speed) == 0 && R(T_speed) == 0);

        /* Property 4: When a bit is being read,
           the sensor should be on Green mode */
        assert(ecrobot_get_nxtcolorsensor_mode(COLOR_SENSOR) == NXT_LIGHTSENSOR_GREEN);
#endif
        /* Read Sensor Value */
        bg_nxtcolorsensor(false);
        color = ecrobot_get_nxtcolorsensor_light(COLOR_SENSOR);
        W(input, color < R(threshold) ? 1 : 0);
    }
}
```

in Reader Task

Properties

Property 1: When a bit is being read, all the motors should **stop**.

Property 2: When writer flips a bit, the tape motor and read motor should **stop**.

Property 3: When tape moves, the writer motor and read motor should **stop**.

Property 4: When a bit is read, the system should be in **read mode**.

Property 5: The sense signal should be high when the tape is moving, not in Reader Task.

```
case WRITE_FLIP:
#ifdef VERIFICATION
    /* Property 3: When writer flips a bit, the tape motor and read
    motor should be stopped. */

    /* IT FAILS!! with BOUND 120 */
    assert(R(T_speed) == 0 && R(R_speed) == 0);
#endif
```

Properties

Property 2: When writer flips a bit, the tape motor and read motor should **stop**.

```
case C_WRITE:
```

```
/* Check if we need to change the bit */
if(R(input) != R(output)) {
    /* Check the header and move it back if necessary */
    if(nxt_motor_get_count(READ_MOTOR) > 0 && R(R_state) == READ_IDLE) {
        W(R_state, READ_MOVE_HEADER_BACKWARD);
    }

    /* Check the header and flip the bit if it is safe to do */
    if(nxt_motor_get_count(READ_MOTOR) <= 0 && R(W_state) == WRITE_IDLE) {
        W(W_state, WRITE_FLIP);
    }
} else {
    /* Nothing to change for writer */
    W(W_state, WRITE_IDLE);
    C_state = C_MOVE;
}
break;
```

Controller
Task

```
case WRITE_FLIP:
```

```
#ifdef VERIFICATION
```

```
/* Property 3: When writer flips a bit, the tape motor and read
motor should be stopped. */
```

```
/* IT FAILS!! with BOUND 120 */
```

```
assert(R(T_speed) == 0 && R(R_speed) == 0);
```

```
#endif
```

Writer Task

Properties

Property 2: When w motor and read motor should **stop**.

Do we need to write?

```
case C_WRITE:
```

```
/* Check if we need to chagne the bit */
if(R(input) != R(output)) {
    /* Check the header and move it back if necessary */
    if(nxt_motor_get_count(READ_MOTOR) > 0 && R(R_state) == READ_IDLE) {
        W(R_state, READ_MOVE_HEADER_BACKWARD);
    }

    /* Check the header and flip the bit if it is safe to do */
    if(nxt_motor_get_count(READ_MOTOR) <= 0 && R(W_state) == WRITE_IDLE) {
        W(W_state, WRITE_FLIP);
    }
} else {
    /* Nothing to change for writer */
    W(W_state, WRITE_IDLE);
    C_state = C_MOVE;
}
break;
```

Controller
Task

```
case WRITE_FLIP:
```

```
#ifdef VERIFICATION
```

```
/* Property 3: When writer flips a bit, the tape motor and read
motor should be stopped. */
```

```
/* IT FAILS!! with BOUND 120 */
```

```
assert(R(T_speed) == 0 && R(R_speed) == 0);
```

```
#endif
```

Writer Task

Properties

Property 2: When writer flips a bit, the tape motor and read motor should **stop**.

```
case C_WRITE:
```

```
/* Check if we need to change the bit */
if(R(input) != R(output)) {
    /* Check the header and move it back if necessary */
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        W(R_state, READ_MOVE_HEADER_BACKWARD);
    }

    /* Check the header and flip the bit if it is safe to do */
    if(nxt_motor_get_count(READ_MOTOR) <= 0 && R(W_state) == WRITE_IDLE) {
        W(W_state, WRITE_FLIP);
    }
} else {
    /* Nothing to change for writer */
    W(W_state, WRITE_IDLE);
    C_state = C_MOVE;
}
break;
```

Controller
Task

If the READ header is up,
Move it back
to avoid collision!

```
case WRITE_FLIP:
```

```
#ifdef VERIFICATION
```

```
/* Property 3: When writer flips a bit, the tape motor and read  
motor should be stopped. */
```

```
/* IT FAILS!! with BOUND 120 */
```

```
assert(R(T_speed) == 0 && R(R_speed) == 0);
```

```
#endif
```

Writer Task

Properties

Property 2: When writer flips a bit, the tape motor and read motor should **stop**.

```
case C_WRITE:
```

```
/* Check if we need to change the bit */
if(R(input) != R(output)) {
    /* Check the header and move it back if necessary */
    if(nxt_motor_get_count(READ_MOTOR) > 0 && R(R_state) == READ_IDLE) {
        W(R_state, READ_MOVE_HEADER_BACKWARD);
    }

    /* Check the header and flip the bit if it is safe to do */
    if(nxt_motor_get_count(READ_MOTOR) <= 0 && R(W_state) == WRITE_IDLE) {
        W(W_state, WRITE_FLIP);
    }
} else {
    /* Nothing to change for writer */
    W(W_state, WRITE_IDLE);
    C_state = C_MOVE;
}
break;
```

Controller
Task

OK, it's safe to write!

```
case WRITE_FLIP:
```

```
#ifdef VERIFICATION
```

```
/* Property 3: When writer flips a bit, the tape motor and read
motor should be stopped. */
```

```
/* IT FAILS!! with BOUND 120 */
```

```
assert(R(T_speed) == 0 && R(R_speed) == 0);
```

```
#endif
```

Writer Task

Properties

Property 2: When writer flips a bit, the tape motor and read motor should **stop**.

```
case C_WRITE:
```

```
/* Check if we need to change the bit */
if(R(input) != R(output)) {
    /* Check the header and move it back if necessary */
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    if(nxt_motor_get_count(READ_MOTOR) <= 0 && R(W_state) == WRITE_IDLE) {
        W(W_state, WRITE_FLIP);
    }
} else {
    /* Nothing to change for writer */
    W(W_state, WRITE_IDLE);
    C_state = C_MOVE;
}
break;
```

Controller
Task

```
case WRITE_FLIP:
```

```
#ifdef VERIFICATION
```

```
/* Property 3: When writer flips a bit, the tape motor and read
motor should be stopped. */
```

```
/* IT FAILS!! with BOUND 120 */
```

```
assert(R(T_speed) == 0 && R(R_speed) == 0);
```

```
#endif
```

Writer Task

NO!

The position of READ header is in safe area (≤ 0),
however it's possible that it is **still moving!**

Properties

Property 2: When writer flips a bit, the tape motor and read motor should **stop**.

```
case C_WRITE:
```

```
/* Check if we need to change the bit */
if(R(input) != R(output)) {
  /* Check the header and move it back if necessary */
  if(nxt_motor_get_count(READ_MOTOR) > 0 && R(R_state) == READ_IDLE) {
    W(R_state, READ_MOVE_HEADER_BACKWARD);
  }

  /* Check the header and flip the bit if it is safe to do */
  if(nxt_motor_get_count(READ_MOTOR) <= 0 && R(W_state) == WRITE_IDLE) {
    W(W_state, WRITE_FLIP);
  }
} else {
  /* Nothing to change for writer */
  W(W_state, WRITE_IDLE);
  C_state = C_MOVE;
}
break;
```

Controller
Task

```
case WRITE_FLIP:
```

```
#ifdef VERIFICATION
```

```
/* Property 3: When writer flips a bit, the tape motor and read
motor should be stopped. */
```

```
/* IT FAILS!! with BOUND 120 */
```

```
assert(R(T_speed) == 0 && R(R_speed) == 0);
```

```
#endif
```

Writer Task

REKH(out tool) can find this bug within 2mins.

DEMO

REKH & Counterexample

<http://www.cs.cmu.edu/~soonhok/rekh-viz>

Thank you!